

# A COMBINED METHOD FOR MEASURING SUPER-HIGH CAPACITORS ABSORPTION CHARACTERISTICS.

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**Abstract** - The paper is devoted to measuring of super-high capacitor energy characteristics with direct current. The authors investigated the mathematical models of super-high capacitors with direct current stable source and proposed new combined method and variation-current method for measuring energy characteristics of super-high capacitors.

**Keywords** - combined method, variation-current method, super-high capacitor, equivalent circuit, energy characteristics, stable current source.

By analyzing the super-high capacitors equivalent circuit, it is possible to make a conclusion: this circuit consists of the  $R_A C_A$  absorption circuits.

Actually, the nature of the real super-high capacitors is much more complicated. The presence of both capacity and losses active resistance are obvious. Besides, they are distributed under the defined law on a length or on a volume of the super-high capacitor constructive space.

Graphically, fragment of the super-high capacitor constructive space can be illustrated by the Nguyen Thien-Chi and J. Vergnolle equivalent circuit, fig.1 [1].

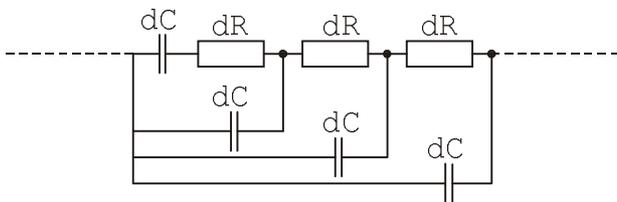


Fig. 1. The Nguyen Thien-Chi and J. Vergnolle equivalent circuit.

The elementary differential capacity  $dC$  circuits are charged through the elementary differential resistance  $dR$  circuits in this equivalent circuit. Depending on a capacitor construction these  $dC$  and  $dR$  circuits are allocated either on a length  $dl$  or on a volume  $dof$  of the capacitor constructive space.

Such approach at the mathematical exposition of real super-high capacitors is the most correct, however, is complicated enough. The transition from differential  $dC$  and  $dR$  elementary circuit to the absorption capacitance  $C_A$  and resistance  $R_A$  equivalent circuits allows experimentally to confirm the considered mathematical capacitor model with a defined accuracy.

The super-high capacitor mathematical model equivalent circuit is shown in fig.2.

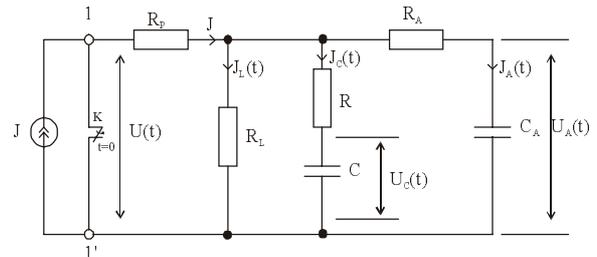


Fig. 2. The super-high capacitor mathematical model equivalent circuit.

In this equivalent circuit:  $R_p$  is the pin resistance;  $R_L$  is the leakage resistance;  $R$  is the active serial resistance;  $C$  is the main capacitance;  $R_A$  is the absorption resistance;  $C_A$  is the absorption capacitance;  $J$  is the stable current course ( $J=\text{const}$ ).

According to this equivalent circuit the authors propose new combined method for measuring of the  $C_A$  and  $R_A$  absorption characteristics. This method is explained by the timing diagram in fig.3.

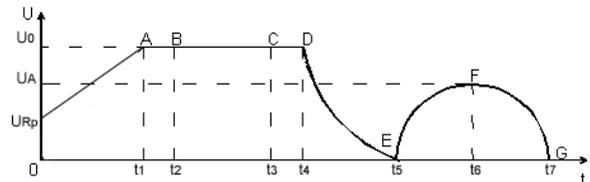


Fig.3. The combined method timing diagram.

The essence of combined method consists of four stages.

- 1) At first the super-high capacitor is charged from stable current source ( $J=\text{const}$ ) to the defined voltage  $U_0$ . By measuring the voltage  $U_{Rp}$  and time  $t_1$  we can define the main resistance  $C$ , the resistance  $R_p$  and  $R$ .
- 2) At the second stage, it is necessary to switch the super-high capacitor to the stable voltage source ( $E=U_0=\text{const}$ ) and to charge the main capacitance  $C$  and absorption  $C_A$  completely.
- 3) At the third stage we discharge the main capacitance  $C$  quickly so that we don't discharged the absorption  $C_A$ .
- 4) After that we have to disconnect the super-high capacitor from source and to wait when the voltage will be equal to maximum value  $U_A$ .

In this case the charge passed from capacitance  $C_A$  to capacitance  $C$ . This process is shown in fig.4.

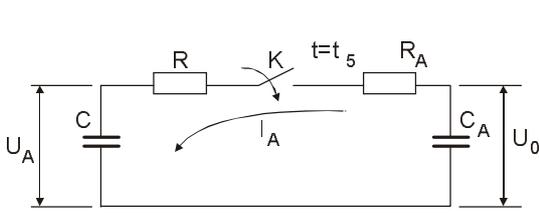


Fig.4. Recharging the capacitance C from capacitance  $C_A$ .

The absorption capacitance  $C_A$  and resistance  $R_A$  can be found out by the expressions:

$$C_A = C \frac{U_A}{U_0 - U_A} \quad (1)$$

$$R_A = \frac{t_6}{C \ln \left( \frac{U_A}{U_0} \right)} - R \quad (2)$$

The proposed method allows to define the electrical parameters of super-high capacitor equivalent circuit fig.2. To measure this parameters authors propose the super-high capacitor analyzer block diagram fig.5.

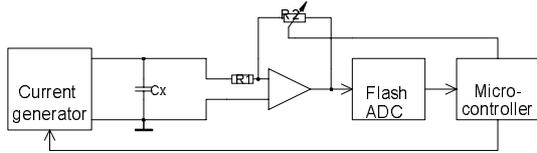


Fig.5. The super-high capacitor analyzer block diagram

During design, manufacture and maintenance of super-high capacitors, there is a problem for monitoring of their energy characteristics. It is important to know not only maximum electrical energy, which can be accumulated by the super-high capacitor, but also its ability to return this energy at different values of load impedance [2].

The knowledge of such performances allows forecasting the ability to support a voltage rating of the super-high capacitor on a load in a given limitation during a particular time interval at different loads. Besides, the determination of a discharge current maximum value of the super-high capacitor and maximum time interval, during which the load voltage will be in necessary voltage range, is important too.

Monitoring of these super-high capacitor energy characteristics gives the answer to a problem, by what maximum enabled current is possible to charge the super-high capacitor and how long it takes.

Also, the self-discharge parameters of such capacitors are important for user application of super-high capacitors.

According to circuit theory, the equivalent circuit for charging super-high capacitor looks like fig.6.

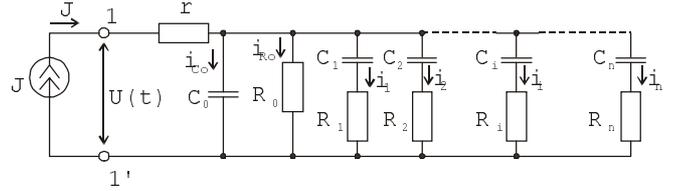


Fig.6. The equivalent circuit for charging of the super-high capacitor by a stable current source  $J = \text{const}$ .

In this equivalent circuit:  $r$  is an equivalent active resistance of losses;  $C_0$  is a geometrical (non-inert) capacity;  $R_0$  is an active leakage resistance;  $R_i C_i$  are  $n$  - relaxation circuits.

The source current  $J$  will be distributed on the currents of the relevant sections of the super-high capacitor equivalent circuit:

$i_{R_0}$  is a current that goes through the resistance  $R_0$ ;

$i_{C_0} = C_0 \frac{\partial U_0}{\partial t}$  is a charge current of the capacity  $C_0$ ;

$i_i = C_i \frac{\partial U_i}{\partial t}$  is relevant current of an  $i$ - section.

Therefore,

$$J = i_{R_0} + i_{C_0} + \sum_{i=1}^n i_i \quad (3)$$

The voltage  $U(t)$  that occurs on pins 1-1' of the super-high capacitor in a time of a charge by the stable current source  $J$ , is determined by expression:

$$U(t) = Jr + R_0 i_{R_0} \quad (4)$$

In this expression the second item is a voltage drop  $U_0$  on a parallel-connected circuits of an equivalent circuit:

$$U_0 = R_0 i_{R_0} \quad (5)$$

Let's differentiate this expression (5), taking into account, that  $\frac{dU_0}{dt} = \frac{i_{C_0}}{C_0}$ :

$$\frac{dU_0}{dt} = R_0 \frac{di_{R_0}}{dt} = \frac{i_{C_0}}{C_0} \quad (6)$$

On the other hand, the voltage  $U_0$  equals to sum of drop voltages of the capacity  $C_i$  and the resistance  $R_i$  of the relevant circuit of absorption.

$$U_0 = U_i + R_i i_i \quad (7)$$

Let's differentiate this expression (7) taking into account, that  $\frac{dU_i}{dt} = \frac{i_i}{C_i}$ :

$$\frac{dU_0}{dt} = \frac{dU_i}{dt} + R_i \frac{di_i}{dt} = R_0 \frac{di_{R_0}}{dt} \quad (8)$$

Taking into account expressions (3)...(8) we shall write a system of a differential equations, that describes the process of a charge of the super- high capacitor by a stable current source J for an equivalent circuit of fig.6.

$$\begin{cases} i_{R_0} + i_{C_0} + \sum_{i=1}^n i_i = I \\ i_i + R_i C_i \frac{di_i}{dt} = R_0 C_i \frac{di_{R_0}}{dt} \\ i_{C_0} = R_0 C_0 \frac{di_{R_0}}{dt} \end{cases} \quad (9)$$

Taking into account, that  $R_0 C_0 = \tau_0$ ,  $R_i C_i = \tau_i$  and  $R_0 C_i = \tau_{0i}$ , it is possible to express the system (9) as:

$$\begin{cases} i_{R_0} + i_{C_0} + \sum_{i=1}^n i_i = \hat{I} \\ i_i + \tau_i \frac{di_i}{dt} = \tau_{0i} \frac{di_{R_0}}{dt} \\ i_{C_0} = \tau_0 \frac{di_{R_0}}{dt} \end{cases} \quad (10)$$

The common decision of an equation system (10) looks like:

$$\begin{cases} i_{R_0} = i_{R_0}^* + i_{R_0}^{**} \\ i_{C_0} = i_{C_0}^* + i_{C_0}^{**} \\ i_i = i_i^* + i_i^{**} \end{cases}, \quad (11)$$

Where  $i_{R_0}^*$ ,  $i_{C_0}^*$  and  $i_i^*$  are complete solutions of a homogeneous system of equations ("free" current components of circuits);

$i_{R_0}^{**}$ ,  $i_{C_0}^{**}$  and  $i_i^{**}$  are partial solutions of an inhomogeneous system of equations ("forced" current components of circuits).

The components  $i_{C_0}^*$  and  $i_i^*$  decrease when time increases. Besides, when  $t \rightarrow \infty$  they come to zero. And the component  $i_{R_0}^*$  increases when time increases. Besides, when  $t \rightarrow \infty$   $i_{R_0}^* \rightarrow J$ .

The components  $i_{R_0}^{**}$ ,  $i_{C_0}^{**}$  and  $i_i^{**}$  at  $t \rightarrow \infty$  characterize steady currents of sections in an equivalent circuit, fig.6.

Taking into account, that the circuit feeds from a source of a stable current I the steady currents of sections accordingly are equal:

$$i_{R_0}^{**} = J, \quad i_{C_0}^{**} = 0 \quad \text{and} \quad i_i^{**} = 0.$$

The solutions  $i_{R_0}^*$ ,  $i_{C_0}^*$  and  $i_i^*$  of a homogeneous system are possible to present as:

$$\begin{cases} i_{R_0} = \sum_l A_{R_{0l}} e^{P_l t} \\ i_{C_0} = \sum_l A_{C_{0l}} e^{P_l t} \\ i_i = \sum_l A_{il} e^{P_l t} \end{cases} \quad (12)$$

If to substitute expression (12) in to a system (10) and to balance expressions for identical exponential curves  $e^{P_l t}$ , we will get a ratio between coefficients  $A_{R_{0l}}$ ,  $A_{C_{0l}}$  and  $A_{il}$ .

$$\begin{cases} A_{C_{0l}} = \tau_0 P_l A_{R_{0l}} \\ A_{il} = \frac{\tau_{0i}}{1 + \tau_i P_l} A_{R_{0l}} \end{cases} \quad (13)$$

We shall substitute expression (12) and (13) for any l in the first equation (10) and we shall reduce  $A_{R_{0l}}$ . Then we shall receive a secular equation for calculation all  $P_l$  of solutions of an equation.

$$1 + \tau_0 P + \sum_{i=1}^n \frac{\tau_{0i}}{1 + \tau_i P} = 0 \quad (14)$$

The index l in the equation (14) is dropped. This equation has l of the radicals and after its solution each of the radicals can assign the index l.

In a general view the expression for the radicals of a secular equation looks like:

$$P = - \sum_{i=1}^n \frac{1 + \tau_{0i}}{\tau_0 + \tau_i + \tau_0 \tau_i} \quad (15)$$

#### Conclusion

By using this mathematical models authors propose the new combined and variation-current methods for measuring the super-high capacitor energy characteristics.

#### REFERENCES

- [1] M. Zakgeim *The Electrolytic Capacitors*, Moscow, 1963-326p.
- [2] F. Grinevich, M. Surdu *Precision variation measuring systems of alternating current*. Kiev, 1989 -192p.